

UNIT I

Taylor's and Maclaurin's Series

- 1) The expansion of $f(x)$ in ascending powers of x about $a = 0$ is
- $f(0) - xf'(0) + \frac{x^2}{2!}f''(0) - \frac{x^3}{3!}f'''(0) + \dots$
 - $f(0) + xf'(0) + \frac{x^2}{2!}f''(0) + \frac{x^3}{3!}f'''(0) + \dots$
 - $-f(0) - xf'(0) - \frac{x^2}{2!}f''(0) - \frac{x^3}{3!}f'''(0) - \dots$
 - $f(0) + xf'(0) + x^2f''(0) + x^3f'''(0) + \dots$
- 2) Expansion of $e^{1/x}$ in powers of x is
- $\frac{1}{x} + \frac{1}{x^2} + \frac{1}{x^3} + \dots$
 - $1 + \frac{1}{x} + \frac{1}{2!x^2} + \frac{1}{3!x^3} + \frac{1}{4!x^4} - \dots$
 - $1 - \frac{1}{x} + \frac{1}{2!x^2} - \frac{1}{3!x^3} + \frac{1}{4!x^4} - \dots$
 - $x - \frac{1}{x} + \frac{1}{x^2} - \frac{1}{x^3} + \dots$
- 3) Expansion of $\log(1 - x^4) - \log(1 - x)$ in ascending powers of x is
- $-x - \frac{x^2}{2} - \frac{x^3}{3} - \frac{3}{4}x^4 + \dots$
 - $x + \frac{x^2}{2} + \frac{x^3}{3} - \frac{3}{4}x^4 + \dots$
 - $x + \frac{x^2}{2!} + \frac{x^3}{3!} - \frac{3}{4!}x^4 + \dots$
 - $-x + \frac{x^2}{2} + \frac{x^3}{3} - \frac{3}{4}x^4 + \dots$
- 4) The coefficient of $\left(x - \frac{\pi}{3}\right)^2$ in the expansion of $\log \cos x$ about $\frac{\pi}{3}$ is
- $-\sqrt{3}$
 - $\sqrt{3}$
 - -2
 - 2
- 5) The expansion of $f(x + h)$ in ascending powers of h is
- $f(h) + xf'(h) + \frac{x^2}{2!}f''(h) + \frac{x^3}{3!}f'''(h) + \dots$
 - $f(x) + hf'(x) + \frac{h^2}{2!}f''(x) + \frac{h^3}{3!}f'''(x) + \dots$
 - $f(h) - xf'(h) + \frac{x^2}{2!}f''(h) - \frac{x^3}{3!}f'''(h) + \dots$
 - $f(x) - hf'(x) + \frac{h^2}{2!}f''(x) - \frac{h^3}{3!}f'''(x) + \dots$
- 6) The coefficient of x^2 in the expansion of $\tan\left(x + \frac{\pi}{4}\right)$ in ascending powers of x is
- 1
 - 2
 - $4/3!$
 - $3!$
- 7) The coefficient of x^{10} in the expansion of $\log(1 - x^2)$ is
- $-1/10$
 - $1/5$
 - $1/10$
 - $-1/5$
- 8) The expansion of $1/x$ about $x = 1$ upto first three terms is
- $1 - (x - 1) + (x - 1)^2 - \dots$
 - $1 + (x - 1) + (x - 1)^2 + \dots$
 - $1 + (x - 1) + \frac{(x-1)^2}{2!} + \dots$
 - $1 - (x - 1) + \frac{(x-1)^2}{2!} - \dots$
- 9) In the expansion of $x^3 + 7x^2 + x - 6$ in powers of $(x - 3)$ the constant term is
- 6
 - 33
 - 87
 - 32

10) The expansion of $\log(1 - x)$ is

- a) $1 + x + x^2 + x^3 + x^4 + \dots$
 b) $1 - x + x^2 - x^3 + x^4 - \dots$
 c) $x + \frac{x^2}{2} + \frac{x^3}{3} + \frac{x^4}{4} + \dots$
 d) $-x - \frac{x^2}{2} - \frac{x^3}{3} - \frac{x^4}{4} - \dots$

11) The expansion of $e^x \log(1 + x)$ is

- a) $1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$
 b) $1 - x + \frac{x^2}{2!} - \frac{x^3}{3!} + \dots$
 c) $x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$
 d) $x - \frac{x^2}{2!} - \frac{x^3}{3!} - \dots$

12) In the expansion of $\sin x$ about $x = \pi/2$, the coefficient of $(x - \frac{\pi}{2})$ is

- a) 0
 b) $1/24$
 c) 1
 d) $1/6$

13) The expansion of $1/(1 + x)$ in ascending powers of x is

- a) $-1 - x - x^2 - x^3 - \dots$
 b) $1 + x + x^2 + x^3 + \dots$
 c) $1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \dots$
 d) $1 - x + x^2 - x^3 + \dots$

14) The coefficient of $(x - 3)^4$ in the expansion of $x^4 - 3x^3 + 2x^2 - x + 1$ in powers of $(x - 3)$ is

- a) 1
 b) -1
 c) 9
 d) -9

15) Expansion of $\sinh x$ in ascending powers of x is

- a) $1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$
 b) $x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots$
 c) $1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \dots$
 d) $x + \frac{x^3}{3!} + \frac{x^5}{5!} + \dots$

16) Expansion of $\cosh x$ in ascending powers of x is

- a) $1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$
 b) $x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots$
 c) $1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \dots$
 d) $x + \frac{x^3}{3!} + \frac{x^5}{5!} + \dots$

17) The n^{th} term in the expansion of e^{-x} is

- a) $x^{n-1}/(n-1)!$
 b) $((-1)^{n-1}x^{n-1})/(n-1)!$
 c) $x^n/n!$
 d) $((-1)^n x^n)/n!$

18) The coefficient of x in the expansion of $e^x \cos x$ is

- a) 0
 b) -1
 c) 1
 d) $1/2$

19) The constant term in the expansion of $\tan^{-1}(\frac{p-qx}{q+px})$ is

- a) $\tan^{-1}(p/q)$
 b) $\tan(p/q)$
 c) $\tan^{-1}(q/p)$
 d) $\tan(q/p)$

20) First two terms in expansion of $\tan^{-1}(1 + x)$ is

- a) $\frac{\pi}{4} + \frac{x}{2} - \dots$
 b) $x - \frac{x^3}{3!} + \dots$
 c) $\frac{\pi}{4} - \frac{x}{2} - \dots$
 d) $x + \frac{x^3}{3!} + \dots$

21) The first three terms in the power series for $\log(1 + \sin x)$ are

- a) $x - \frac{1}{2}x^3 + \frac{1}{4}x^5$
 b) $x + \frac{1}{2}x^3 + \frac{1}{4}x^5$
 c) $-x - \frac{1}{2}x^3 + \frac{1}{4}x^5$
 d) $x - \frac{1}{2}x^2 + \frac{1}{6}x^3$

- 22) In the Taylor series expansion of $e^x + \sin x$ about the point $x = \pi$ the coefficient of $(x - \pi)^2$ is
- e^π
 - $0.5e^\pi$
 - $e^\pi + 1$
 - $e^\pi - 1$
- 23) Which of the following functions would have only odd powers of x in its Taylor series expansion about the point $x = 0$.
- $\sin(x^3)$
 - $\sin(x^2)$
 - $\cos(x^2)$
 - $\cos(x^3)$
- 24) The limit of the series $f(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots$ as x approaches $\frac{\pi}{2}$ is
- $2\pi/3$
 - $\pi/2$
 - $\pi/3$
 - 1
- 25) The Taylor series expansion of $\frac{\sin x}{x - \pi}$ at $x = \pi$ is given by
- $1 + \frac{(x - \pi)^2}{3!}$
 - $-1 - \frac{(x - \pi)^2}{3!}$
 - $1 - \frac{(x - \pi)^2}{3!}$
 - $-1 + \frac{(x - \pi)^2}{3!}$
- 26) Expansion of $\log(1 + x + x^2 + x^3 + x^4)$ is
- $-x - \frac{x^2}{2} - \frac{x^3}{3} - \frac{x^4}{4} - \dots$
 - $x + \frac{x^2}{2} + \frac{x^3}{3} + \frac{x^4}{4} - \dots$
 - $x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots$
 - $x + \frac{x^2}{2} + \frac{x^4}{3} + \frac{x^5}{4} - \dots$
- 27) Expansion of $\sin x \cosh x$
- $x + \frac{x^3}{3} + \frac{x^5}{30} + \dots$
 - $x - \frac{x^3}{3} - \frac{x^5}{30} + \dots$
 - $x + \frac{x^3}{3} - \frac{x^5}{30} + \dots$
 - None
- 28) Expansion of $\log\left(\frac{\tan x}{x}\right)$
- $\frac{x^2}{3} - \frac{7}{90}x^4 + \dots$
 - $-\frac{x^2}{3} - \frac{7}{90}x^4 + \dots$
 - $x + \frac{x^2}{3} - \frac{7}{90}x^4 + \dots$
 - $\frac{x^2}{3} + \frac{7}{90}x^4 + \dots$
- 29) Expansion of $\sin(e^x - 1)$ is
- $x + \frac{x^2}{2} - \frac{5}{24}x^4 + \dots$
 - $x + \frac{x^2}{2} + \frac{5}{24}x^4 + \dots$
 - $x - \frac{x^2}{2} - \frac{5}{24}x^4 + \dots$
 - None
- 30) The limit of the series $f(x) = 1 - x + x^2 - x^3 + x^4 - \dots$ as x approaches $\frac{1}{2}$ is
- $\frac{2}{3}$
 - $\frac{1}{3}$
 - 1
 - $\frac{4}{3}$
- 31) The limit of the series $f(x) = 1 + x + x^2 + x^3 + x^4 + \dots$ as x Approaches $\frac{1}{2}$ is
- 4
 - ∞
 - 3
 - 2

- 32) Representation of $(x-2)^4 - 3(x-2)^3 + 4(x-2)^2 + 5$ in powers of x is
- $61 - 84x + 4x^2 - 11x^3 + x^4$
 - $61 + 84x - 4x^2 - 11x^3 + x^4$
 - $61 + 84x + 4x^2 - 11x^3 + x^4$
 - $61 + 84x + 4x^2 - 11x^3 - x^4$
- 33) The first three terms in expansion of $x^4 - 3x^3 + 2x^2 - x + 1$ in powers of $(x-3)$ is
- $16 - 38(x-3) + 29(x-3)^2$
 - $16 + 38(x-3) - 29(x-3)^2$
 - $16 - 38(x-3) - 29(x-3)^2$
 - $16 + 38(x-3) + 29(x-3)^2$
- 34) The Maclaurin series of $f(z) = 1/(1+z^2)$ is
- $1 - z^2 + z^4 - z^6 + \dots$
 - $1 + z^2 + z^4 + z^6 + \dots$
 - $1 - z^2 - z^4 - z^6 + \dots$
 - None
- 35) $\lim_{x \rightarrow 1} \frac{x-x^x}{1+\log x-x}$ is
- 0
 - 1
 - ∞
 - 2
- 36) If $\lim_{x \rightarrow 0} \frac{\sin 2x + p \sin x}{x^3}$ is finite then the value of p is
- 0
 - 1
 - 2
 - 2
- 37) $\lim_{x \rightarrow 0} \frac{\log(\tan x)}{\log x}$ is
- 0
 - 1
 - 1
 - 2
- 38) $\lim_{x \rightarrow 0} \frac{\log(\sin 2x)}{\log(\sin x)}$ is
- 0
 - 1
 - 1
 - 2
- 39) $\lim_{x \rightarrow 0} x \log x$ is
- 0
 - 1
 - 1
 - 2
- 40) $\lim_{x \rightarrow 0} \left(\frac{1}{x} - \frac{1}{\sin x}\right)$ is
- 0
 - 1
 - 1
 - 2
- 41) The value of $\lim_{x \rightarrow 2} \frac{xe^{-x} - 2e^{-2}}{x-2}$ is
- e^{-2}
 - 1
 - $-e^{-2}$
 - 1
- 42) The value of $\lim_{x \rightarrow \infty} \left(\frac{1}{x}\right)^{1/x}$ is
- 1
 - 0
 - 1
 - 2
- 43) The value of $\lim_{x \rightarrow 0} \log_{\tan x} \sin x$ is
- 1
 - 0
 - 1
 - 2
- 44) The value of $\lim_{x \rightarrow 0} \sin x \log x$ is
- 1
 - 0
 - 1
 - 2
- 45) The value of $\lim_{x \rightarrow 0} x \log \sin x$ is
- 1
 - 0
 - 1
 - 2
- 46) The value of $\lim_{x \rightarrow y} \frac{x^y - y^x}{x^x - y^y}$ is
- $\frac{1-\log y}{1+\log y}$
 - $\frac{1+\log y}{1-\log y}$
 - $\frac{1-\log y}{-1-\log y}$
 - $\frac{1+\log y}{-1-\log y}$
- 47) The value of $\lim_{x \rightarrow 0} \frac{(1-x)^n - 1}{x}$ is
- 0
 - n^2
 - $-n$
 - 1

Indeterminate form

85) If $f(x)$ and $g(x)$ are 2 functions such that $f(a) = 0$ and $g(a) = 0$ then

$\lim_{x \rightarrow a} \frac{f(x)}{g(x)}$ is equal to

- a) $\lim_{x \rightarrow a} \frac{f''(x)}{g(x)}$ b) $\lim_{x \rightarrow a} \frac{f(x)}{g'(x)}$
 c) $\lim_{x \rightarrow a} \frac{f'(x)}{g(x)}$ d) $\lim_{x \rightarrow a} \frac{f'(x)}{g'(x)}$

86) The value of $\lim_{x \rightarrow 0} \frac{a^x - 1}{x}$ is

- a) a b) $\log a$ c) $\log e$ d) e

87) The value of $\lim_{x \rightarrow 0} \frac{\cosh x - \cos x}{x^2}$ is

- a) 0 b) ∞ c) 1 d) -1

88) If $\lim_{x \rightarrow 0} \frac{x(1+a \cos x) - b \sin x}{x^3}$ then

- a) $b - a = 1$ b) $a - b = 1$
 c) $a - b = 0$ d) $a - b = 3$

89) $\lim_{x \rightarrow 1} \frac{f(x) - 2}{f(x) + 2} = 0$, then $\lim_{x \rightarrow 1} f(x)$ is equal to

- a) 1 b) -1 c) -2 d) 2

90) $\lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1}$ is equal to

- a) ∞ b) 0 c) 2 d) 1

91) $\lim_{x \rightarrow \infty} \frac{x^3 - \cos x}{x^2 + (\sin x)^2}$ is equal to

- a) ∞ b) 0 c) 2 d) 1

92) $\lim_{x \rightarrow 3} \frac{2x^2 - 7x + 3}{5x^2 - 12x - 9}$ is equal to

- a) $-1/3$ b) $5/18$ c) 0 d) $2/5$

93) $\lim_{n \rightarrow 0} e^{-\frac{n}{\log n}}$ is equal to

- a) 1 b) -1 c) 0 d) *does not exist*

94) $\lim_{n \rightarrow 0} 8^{-\frac{n}{\log n}}$ is equal to

- a) 1 b) -1 c) 0 d) *does not exist*

95) $\lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)^{\frac{1}{n}} \left(1 + \frac{2}{n}\right)^{\frac{1}{n}} \dots \left(1 + \frac{n}{n}\right)^{\frac{1}{n}}$ is equal to

- a) 1 b) $2/e$ c) $3/e$ d) $4/e$

96) $\lim_{x \rightarrow 0} \frac{\sin^2 x}{x}$ is equal to

- a) 0 b) ∞ c) 1 d) -1

97) $\lim_{x \rightarrow \infty} \frac{\log x}{x^n}$, $n > 0$ is equal to

- a) 0 b) ∞ c) 1 d) -1

98) $\lim_{x \rightarrow \infty} \frac{x^m}{e^x}$, $m > 0$ is equal to

- a) 0 b) ∞ c) 1 d) -1

99) $\lim_{n \rightarrow 0} 5^{\frac{n}{\log n}}$ is equal to

- a) 1 b) -1 c) *does not exist* d) 0

100) $\lim_{x \rightarrow \infty} \frac{x^m}{e^{x+2x^3}}$, $m > 0$ is equal to

- a) 0 b) ∞ c) 1 d) -1

101) $\lim_{x \rightarrow \infty} \frac{x^m}{e^{5x-3x+78}}$, $m > 0$ is equal to

- a) 0 b) ∞ c) 1 d) -1

102) The value of $\lim_{x \rightarrow 0} \left(\frac{1^x + 2^x + 3^x + 4^x}{4}\right)^{\frac{1}{x}}$ is

- a) $(24)^{1/4}$ b) 24 c) 10 d) $(6)^{1/4}$

103) The value of $\lim_{x \rightarrow \infty} x^{55} e^{-2x}$ is

- a) 1 b) 0 c) ∞ d) *none of these*

104) The value of $\lim_{x \rightarrow 0} \frac{\sin x}{x}$ is

- a) 1 b) -1 c) -3 d) 0

105) The value of $\lim_{x \rightarrow 0} \frac{(1+x)^n - 1}{x}$ is

- a) 1 b) $n - 1$ c) n d) *none*

106) The value of $\lim_{x \rightarrow 0} \frac{(1+x)^5 - 1}{x}$ is

- a) 1 b) 4 c) 5 d) *none*

107) The value of $\lim_{x \rightarrow 0} \frac{(1+x)^9 - 1}{x}$ is

- a) 1 b) 8 c) 9 d) *none*

Unit - IV

Taylor's & Maclaurin's Theorem , Indeterminant Form

Answer Key

Q.No.	Ans	Q.No.	Ans	Q.No.	Ans	Q.No.	Ans
1	b	28	d	55	b	82	b
2	b	29	a	56	a	83	a
3	b	30	a	57	c	84	A
4	d	31	d	58	b	85	d
5	b	32	c	59	d	86	b
6	c	33	d	60	c	87	c
7	a	34	a	61	b	88	a
8	d	35	d	62	a	89	d
9	c	36	c	63	c	90	c
10	c	37	b	64	b	91	a
11	c	38	c	65	a	92	b
12	a	39	a	66	b	93	d
13	d	40	a	67	d	94	d
14	a	41	c	68	a	95	a
15	d	42	b	69	a	96	a
16	c	43	c	70	a	97	a
17	b	44	b	71	c	98	a
18	c	45	b	72	a	99	c
19	a	46	a	73	b	100	a
20	a	47	c	74	c	101	a
21	d	48	a	75	d	102	a
22	b	49	b	76	b	103	b
23	a	50	b	77	c	104	a
24	d	51	c	78	b	105	c
25	d	52	d	79	a	106	c
26	b	53	c	80	c	107	c
27	c	54	b	81	b		